&RGH 1R

1DPH

6HFRQG < HDU ± 0DUFK

7LPH +RXU\
&RRO RII WLPH 0

3DUW ± ,,, &+(0,675 < 0D[LPXP 6FRUHV

```
*HQHUDO,QVWUXFWLRQV WR &DQGLGDWHV
 x 7KHUH LV D µ&RRO RII WLPH¶ RI PLQXWHV LQ DGGL
 x 8VH WKH µ&RRO RII WLPH¶ WR JHW IDPLOLDU ZLWK T
 x 5HDG TXHVWLRQV FDUHIXOO\ EHIRUH DQVZHULQJ
 x 5HDG WKH LQVWUXFWLRQV FDUHIXOO\
 x &DOFXODWLRQV ILJXUHV DQG JUDSKV VKRXOG EH VI
 x ODOD\DODP YHUVLRQ RI WKH TXHVWLRQV LV DOVR SI
 x *LYH HTXDWLRQV ZKHUHYHU QHFHVVDU\
 x (OHFWURQLF GHYLFHV H[FHSW QRQ SURJUDPPDEOH F
   ([DPLQDWLRQ +DOO
39% e8; •9 Áh; • > (8#; '9; ?:f
 x '9 \cite{t} f 9 \cite{t} 6, -q 9' D (;/9,'9,D <\chi>0) D 08-9.9h; í
   <Á 8)D >> ? 8%ejÁ (.9 -> t 8'; q.jÁ
                                            6 < f # "
   > w8'; (?-89h; i)
 x q.jÁ 2;#;s#9'D,:uD 8%ejÁ — "8(<;x 38-9h" í
 x '9; ?f4jA, ;2;3'; -"8(<;x 38-9h" í
   "hD <n0, Áì 9f#jÁì f8); Áì s93 q.?(t/9Å #>s
    o8-9.9h" í
 x ? 8%ejÁ ,0-81q90; '°9-9n;oD
   x ? f(8f 8,; A) > w8'8 8q 8Ah;?0,/; A 29>-|; \bullet
    0 D?f 8"9 D (."3; (.:d87819À (?-8 9h;38¾ (8 9yí
```

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4XHVWLRQV WR &DUU\RQH VFRUH HDFK $QVZHU
:KDW LV WKH FR RUGLQDWLRQ QXPEHU RI SDUWLFOHV
```

,GHQWLI\ WKH RUGHU RI UHDFWLRQ♥LI WKH XQLW RI UI

:KDW LV WKH VWUXFWX&H"RI FKURPDWH LRQ &U2

1 DPH WKH WHVW XVHG WR LGHQDWQLG\HSWUKLPQRODFLQHV

:KLFK DPRQJ WKH JLYHQ YLWDPLQV LV ZDWHU VROXEO

D \$

E %

F '

G (

:KDW LV WKH FURVVOLQNHG SRO\PHU REWDLQHG E\IRUPDOGHK\GH "

BBBBBBBB LV DQ DUWLILFLDO VZHHWQHU ZKLFK LV X

4XHVWLRQV WR \$QVZHU DQ\ WHQ (DFK TXHVWLR 6FR**u**HV

D %DVHG RQ WKH QDWXUH RI LQWHUPROHFXODU IRU L 6L2

LL , FH 6FRUH

E =Q2 WXUQV \HOORZ RQ KHDWLQJ :K\ " 6FRUH

\$ VROXWLRQ FRQWDLQV J *X USHHDU 19 1R 60V 1DU UH PRD WWROXW JL KDV WKH VDPH RVPRWLF SUHVVXUH DV D VROJK 100V LRQ RIZDWHU &DOFXODWH WKH PDVV RIJOXFRVH 69 FURHUVHHVQW L

'HILQH PLQLPXP ERLOLQJ D]HRWURSHV ZLW6KFHUB17SOH

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,;#À ± 3>. ? 8%ejÁhD 8?.8s9'; 8?.8 ?Ÿ8¿ 3:#í
? 8\% e j \acute{A} h; q.>, 2; #; í
                                     ?Ÿ8¿6 Du
)&& 9¥0:- '-;> 9•8' j1;> ? 86; 9?'5¾ 6 e
f # "
?/,D •9.8iq9>¤ -<P'B(€D♥ - .; .86f(3¿q'q9>¤ 8¿ ¿
#9.9k/9-; í
& + & -; q?'8 Å ? \neq q.2+ (?-8 9 k \rightarrow > f(,/9 ,:'; > 1
#9.9k/9-;s (.:d"q9>x ?(.D 2;#; í
D
 Ε
     %
 F
 G
)9?'81; i?)8; ,8 A 9>>7; ?(819>,>>/?65 % 'q9-8 A 0+
(.6, *Ž9# ?(819,;" #D
(8 > w83; s B59 A • 9.# - 9 y8q)
.863±;38 "BDBBBBBBBBBBB.
        3 > . ? 8 \% e j 1 9 Å 8? 8 s 9 ?; Ÿ 8. <math>\wp D3 : \# i > \# i 9 0;
(>qpq9'; q.>,2;#; í
                                   ?Ÿ8¿6Du
 D \# ^{TM} 8 f \# 1; > (.6^*, \check{Z} | q9 > m 6 g + 83 q9 > m 9 \cdot 8 | q9 \grave{A}
   \#8>2>8; q9.9h; s.3±; hÁ \#. \#9.9h; í
        6 L 2
                                           ?Ÿ8;
   LL ,FH
 E < 8h9 - 8 = AQ2m'9/.8 : s:i r:> 80D
                                           ?Ÿ8;
   J</9-è?,819h;18;,816ÐRO; 09,; 0q9Å 0-9t9k
08-'9h; i {<?h86D è?,819h;18 ½ iP,R308 D 0:- 08-'9h;
?. 8 ?86n¹9 D¿ f , 8 "; • # Dí i 9 À { < ? h 8 6 9 > ¤ .; 0 9 , ¿
                                                      0
08-'9-9À j9-9.9h;s {<?h869> m 13D "h8ħŸ&;6D
,9'9, ?*8-90969D?-8?f8t;Á >rsD %87." 679#
                                          ?Ÿ8¿6D
'9¿x 9h; í
                                               3 7 2
```

:ULWH WKH FKHPLFDO HTXDWLRQ RI WKH IROORZLQJ U

D 3UHSDUDWULRR RQ;RHI);H2

6FRUH

E OL[LQDGSGV); H

6FRUH

([SODLQ KRZ WKH FRPSOH@HVDQRGI Q1L@FNSWEIDDYH>1GLLKIHHUH0 VWUXFWXUHV EXW GR QRW GLIIHU LQ WKHL6UFRPUDHJNQHWL

&RPSOHWH WKH UHDFWLRQ

D &#%⊌^{\$}↓[&]1 BBBBBBBB

6FRUH

6FRUH

'XULQEJHWOK PILQDWLRQ UHDFWLRQ RI EURPRSHQWDQH UHVXOWV 3HQW HQH DV PDMRU SURGXFW DQG 3HQW H[SODLQ WKH UHDFWLRQ 6FRUHV

\$URPDWLF DOGHK\GHV XQGHUJR HOHFWURSKLOLF VXIUHDFWLRQ RI EHQ]DOGHK\GH ZLWK FKHPLFD60FRHUTHXVDWLR

%ULHIO\GHVFULEH *DWWHUPDQ .RFK UHDF6WFIRRUQHV

+RZ FDQ LW FRQYHUW PHWK\O LRGLGH WR 6H-WR KUDHQ DPLC

6WDWH WZR GLIIHUHQFHV EHWZHHQ JOREX60FDRW 1910QG IL

ODWFK WKH TROORZLQJ

_				
D	3RO\DFU\ORQLWULOH	L	7 H U \ C) H Q H
Е	%XWDGLHQ \$FU\ORQLWULOH		LL	1 D W X
F	(WK\OHQH JO\FRO 7HUHSKWKDOLI	F DFI	_G L	.LL 9
G	FLV SRO\LVRSUHQH	LY	6\$FRWLH	D/D Q

D :KDW DUH GUXJV "

6 F R U H

E :ULWH DQ H[DPSOH IRU D GUXJ FODVVL6LFHRGJHEDVHG

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\#8>2>8; q9.9h; s.86 f(3; q'j1; > .86 6,38 e 2; #; í
     D; (\mathbf{A}) '9s;; (\mathbf{H}2 - \mathbf{I}) '9; (\mathbf{A}) '9; (\mathbf{
                                                                                                                                                                                             3 Y 8 Y
                                                                                                                                                                                             ?Ÿ8;
                     3 W); H 0; q; s; í
     Е
'9h09>¤ 6-;^j18- >1L &@ + >1L &@2
   ' 18>"i90; 8r9 6g+83q9À 3e#e86 39496#D.9h; í
  '9hÀì?,8,9'Du;
                                                                                                                                                                                       ?Ÿ8;6D
.86 f(3;q' (<;q: .9h;
                      &+%U$J&1 BBBBBBBBB
                                                                                                                                                                                             ?Ÿ8;
                      ?Ÿ8;
           EURPRSHQW/DQHAh?27+819 008-'9-;,8-9 ? ξsqDs
E 09,9?'5\frac{3}{4} f(3\frac{1}{2}q', \frac{1}{3}0lQW f(H8Q8H \frac{1}{3}0,8-; \frac{1}{3}14QW HQH
f(\&8' \$), 8-; 0+9h; s; i E f(3;q' 394%: .9h; s'9-,
f(±839h;
                                                                                                                                                                                      ?Ÿ8;6D
 ?.8,8,9 D \dot{A} 9>>7; \dot{A} ?0 8)909 D \dot{Y} 96, \dot{Y} 6 C 5 \dot{Y}
f(3;q')A 8"9h;s;í >* 3/468A 9>>7 9> p >>'?f 53/4
.86f(3;q' .86 6,38 e,8-9 2;#; í
                                                                                                                                                                                     ?Ÿ8¿6D
n;,8% 8kD86f(3;q';.;h9 394%: .9h; í ?Ÿ8;6D
>2-f)(f8°n6:D; 1; #v90;• .oD 3e#e86jÁ
?{8*;08; ?f(8n:'; 1;
   2;#; í
                                                                                                                                                                                       ?Ÿ8;6D
```

	, (0							
D	3 R O \ D	FUORQLWU	LOH		L	7 H U \ (HQHC	
Е	% 2	KWDGLHQ \$F	U \ O F	QLWULOH		LL	1 D W	Χ
F	(WK\O	HQH JO\FRO	7HL	HSKWKDOL	F DFL	G L	LLL	%
G	FLV	SRO\LVRS	UHQ	Н	LY	\$FUL	O D Q	
	l			l	? Ÿ	′8;6D		

```
D,.;s; Á s8À rD" ?Ÿ8;
E.86 '-;> 9•8'q9À #. #9.9k,.;s; ÁhD.; %87."
2;#; í ?Ÿ8;
```

6FRWHV

\$Q HOHPHQW FU\VWDOOLVH∜ DWVJ&X&QZLWWFKHGHQKVDWLQJ î * FP &DOFXODWH WKH PRODU_sPDVV Rîl **W R G** HOHPHQ 6FRUHV

:ULWH WKH DQRGH DQG FDWKRGH UHDFWLRQV RFFXU OHQWLRQ WKH HOHFWURO\WH XVHG LQ WKH6ERWMWHU\

)RU K\GURO\VLV RI PHWK\O DFHWDWH LQ DTXHRXV \ REVHUYHG

WV		
& + & 2 2 & +		
& PR*O /		

6KRZ WKDW LW IROORZV SVHXGR ILUVW RUGHU UHDFW FRQVWDQW 6FRUHV

6WDWH +DUG\ 6FKXO]H UXOH ZLWK WKBIFIRHUCHSV RI H D :K\ O\RSKLOLF FROORLGV DUH XVHG DV6588WHFWL

*LEEV HQHUJX R*I IPRIUPP JD2DWQLQ Q&D2W . DQG . DUH JL

EHORZ

 $'_1$ * > 0 J 2@ ± N -D PWR O .

 $'_1$ * > & 2@ ± \dagger N - D \dagger VR O

',* > 0 J 2@ ± †N-DPWRO.

 $'_1$ * > & 2@ ± \dagger N -D \dagger WR O

2Q WKH EDVLV RI WKH DERYH GDWD SUHGLFW WKH WH UHGXFLQJ DJHQW IRU 0J2 6FRUHV

```
,; \# A 3>. ? 8\% ej 19A > 2pq9'D q.>, 2; \#; i 8?.8s9';
                                                   ?Ÿ8;6Du
, < s D Y 8 ¿ í
.; ,<0) & & -8-9 f 9 \( \) 0 : .9 h > t n ? t 8 \( \) # 9 > \( \) 6 8 f J # F P
-9 f 9 \pm 0 9 \text{ Å} - < \% 96 \ \cancel{p}9 > \% f ': 1 î \pm FP i 9 \text{ Å} , < 0 q 9 > \%
?,818;,8'66Bh; ≰1 î P₹O
                                                         ?Ÿ8;6D
> 0 D ?\forall 8?\forall D\forall 8,\forall 9-9>0 ?\forall 8 9>0-; 8?\forall 8?\forall 8 9>0-; .86
f(3 \nmid q' | jA) = 2; \#; i *8,/9-9A) = (?-8.9h; s?f08D>0>B*sD
2;#; í
                                                          ?Ÿ8¿6D
,:>>\# Å 69?,,9>\# 0:- 08-'9>- >>7?'f \#91-9?\#8\#D0+9k
'9.:d"jÁ ;3> ? ¿q9.9h;s;í
 WV
 & + & 2 2 & +
 & PR*O /
 0q9> p 8!# •9. 6 e-8-9 #; .;s;>3iA
                                                           f(3;q'
6e<? 8 )¥D 8; ; f(3;q',8>>#"1s$D-9h; í →
                                                         ?Ÿ8;6D
  D78; 95e < A6D '9-, %87."679# f(±839ThY8;6D
 E 0?-8)909>D8?18-9; Á r;>808fD8>n©:38D18-9;
     18-9 (?-8 > t;q;s\#D
                                                           ?Ÿ8;
      .E 58 3 9 0; . E 58 3 9 0 \circ Ji2 _{V} > ^{x} - ; & 2 _{J} > ^{x} - ; 9 * Df \circ D
 '; 9 8)D?)8;7;5*3/4#8>2 > 8;h;s;
', ^* > 0 J 2, ^{\circ} \pm ^{\circ}N - D RVR O .
',* > & 2@ ± N -DRVR O
'_1* > 0 J 2 @ ± \daggerN - D \daggerVR O .
'_1* > & 2@ ± \daggerN - D \daggerVR O .
,; 19 \text{ Å} 6 < 9 \text{ t} 9 \text{ k} 390 1; > 9 \cdot 8 \cdot 9 \text{ Å} 8 3 \# 9 \text{ D} 0 8 \text{ EQS} 2_{\text{V}} > \text{m}
'9?.8: 18.9-8-9 8; *1/2 (?-8 9h>ít ; s # D
                                                         ? Y 8 ¿ 6 D
```

3 7 2

- D :KDW LV WKH IRUPXOD RI SKRVSKLQH "6FRUH

 E +RZ SKRVSKLQH LV SUHSDUHG LQ ODERSUFRW\"
- \$VVLJQ WKH SRVVLEOH UHDVRQ IRU WKH IROORZLQJ
- D 6WDELOLW\RI R[LGDWLRQ VWDWH GHFUHDVHV GRZQ WGRURXS HOHPHQWV 6FRUH
- E 2+LV OHVV D16LGLF WKDQ + 6FRUH
- F 3+2 DFW DV D JRRG UHG3X2FLGORJH10 JOHRQWW ZK6.10 RHU+H
- *LYH UHDVRQV IRU WKH IROORZLQJ
- D 7UDQVLWLRQ PHWDOV DQG PDQ\RI WKK**KER**UFHRPSRX
- F: ULWH WKH VWHS LQYRO&YUH2OGULROP WFKURSPULBHWSHDIBIDIW LR
- +RZ ZRXOG \RX DFFRXQW IRU WKH IROORZLQJ
 - D \$OGHK\GHV DUH PRUH UHDFWLYH WKDQ NHWRQ UHDFWLRQ 6FRUH
- E %RLOLQJ SRLQW RI DOGHK\GHV DUH OR6ZFHRUU MV KDQ
- F \$GGLWLRQ UHDFWLRQ RI VRGLXP K\GURJHQ VXO SXULILFDWLRQ RI DOGHK\GHV 6FRUH
- 4XHVWLRQV WR \$QVZHU DQ\ WKUHH (DFK TXHV)
 6FRWHV
- D :KDW DUH SULPDU\ EDWWHULHV " 6FRUH
- E 7KH FHOO SRWHQWLDO RI D PHUFXU\ FHOO LV *LYH UHDVRQ 6FRUH
- F : ULWH WKH HTXDWLRQV RI WKH UHDF±W2LIRXQHVO LQYR FHOO 6FRUHV

```
? Ÿ 8 ¿
    D?)86D>>)> m .8638 e rD
   E (.:d"480-9 \text{ Å}?)86 \text{ D})^{3/4} '9 \text{ i} v9 \text{ h}; \text{s} > \#\text{i} > "?"8 \text{ i} 6 \text{ D}
#8>2 > 8; q9.9h; s3-; > 8." 6 < 9t9h;
   D 8 f < t; , < 0 j 1 9 Å <math>f < t 9'; , ; 1 9 Å '9 s; \# 8 ? 2 h; 3 . ; ? r
            8 :» . " 8 3 • - ; > • 9 . # ; / - ; - ; - ; > • 9 . #
                                                                                                                                      < ; -;
                                                                                                                                          ? Ŷ 8 ¿
         > W;S;í
                                                                                                                                         ?Ÿ8;
   E 6+> h81; \sim 6g+83 ;/m6-;^+82"D
   F 3+2 .; 'y '9?.:88 × 9 - 8í" Ds 8 À+ 32 '9?.8: 18.9
                                                                                                                                       У
                                                                                                                                          3 8 Ÿ S
  8." 8"9h;
   D 6 f, "?087j1; 3-;> 90 6 -; ^{\hat{}}j1; \hat{A}? f(. j18 "D)
                                                                                                                                          ?Ÿ8;
   E \ddot{Y} 8 = 3e = 3e = 8.\% 83 \cdot 8"9h8 = 9.; s9n; .;
         6 f ," ,<0 ,8-9 "h8h;s;
                                                                                                                                         ?Ÿ8;
   F ?f 8>>,,D -9.9 À1 D& 52 9; v 9 h; s 3 9 &
                                                                                                                                2:#:?Ÿ8;
#8>2 > 8 ; q9.9h; s3>- j>' 390-9.; q8
   D'e<z9?-8)909 D 95¾ f(3;q'j19Àì
                                                                                                                                     \dot{A} 9 >> 7 : \dot{A} \dot{A}
            :?,8"; > 1h8 \acute{A} f(3/q',93; 8"9h;s;
                                                                                                                                       ?Ÿ8;
   E Àh?781; >1h81; #91'90 ;/À389">D>7 ; ÁhD
                                                                                                                                         ?Ÿ8;
                                       >71 % 6\dot{A}>>),;,8-;• :5% f(3\dot{c}q') \dot{A} 9
          >>7; 1; > ?3, #9.9h09'; 4;": ."q9'; (?-8\,\,\,\,\)8\,\;s;\(i\)
     .; \# A = 3 > .-; \bullet ? 8\% e i 19 A > \# i 90; , <> s pop.9 \( -\), \( D2; \# ; \) \( i = 19 A =
  8?.8s9'; '80; ?Ÿ8¿í
                                                                                                                     ?Ÿ8¿6 Du
    D > f(,/9 *8,/9 \acute{A} s8 \grave{A} " rD
                                                                                                                                        ?Ÿ8;
   E .; >, \frac{1}{2}h; \frac{1}{9} > \frac{6}{9} > \frac{9}{9} > \frac{9}{9} > \frac{9}{9} > \frac{9}{9} = \frac{9}{9} > \frac{9}{9}
         F \pm 2) e < 3 Å > 6 y 9 > 0 8?.?8f 80; D1 90;,;• .86 6,38 e
            2;#; í
                                                                                                                                     ?Ÿ8;6D
                                                                                                                                                     3 7 2
```

- D 'UDZ WKH VWUXFWXUHV RIJBUR ®HWULF60FOR UMRPHU
- E: ULWH WKH IRUPXOD RI SHQWDDPPLQHF6DFUREURHQDWR
- F : ULWH DQ\ WZR OLPLWDWLRQV RI YDODQFFRHUERQG \
- D *ULJQDUG UHDJHQWV DUH LPSRUWDQW FODVV R SUHSDUH DOFRKROV ,GHQWLI\ WKH FRPSRXQGV \$ D(

E :ULWH WKH QDPH RI SURGXFWV IRUPHG ZKHQ VD DQK\GULGH LQ DFLG PHGLXP 6FRUHV

/XFDV WHVW LV XVHG WR LGHQWLI\ SULPDU\ VHFRQGD

- D ([SODLQ WKH SURFHVV
- E 1DPH WKH UHDJHQWV XVHG LQ WKH WH6VFWRUHV

BBBBBBBBBBB

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D >) H &1 + @ #.; s 9? - 8 >, f 9 h A > ?68 >, /; 1; >
                                        ?Ÿ8;6D
  3.-; í
 E .8638 e 2;#; í
   3HQWDDPPLQHFDUERQDWRFREDOW ,,, ?FŸK8O;RULGH
 F 380 3/4 610 * 8 o D 69 "8 r q 9 > p . o D 2/4 (828, #1; í ? Ÿ 8 ¿
 D Ah?781; 1; > '9¿v8"q9A (?-8 9h; s f(&8' .863±;
  h18"D f 9 D/98?;- Dx; Ásí %s93 #9.9k/9mD .8638 e
   2;#; í
        + & + 2 0 J & + • • • • 0 H W K H U 2 + % U
        E 680969096 D 6,9 D½>>7>>f 9>x ~08-'9-;,8-9
  ? ¿s8À 0+9h;ssq9>¤ ?(>.2;#; í
                                       ?Ÿ8;6D
>>f(,/9) > 6h m/9)? 5e/9 Ah?781; >1 #9.9k/9-;s#9';(
h;s .; (.:d",8"D0<h86D (.:d" í
D(.:d" 393.9h; í
 E(.:d"q9Å(?-8.9h;s.863\pm;h1;>
                                 ?(>.2;#ÿ8;6D
                  BBBBBBBBBBBB
```